Impact of compression on gas transport in non-woven gas diffusion layers of high temperature polymer electrolyte fuel cells

Dieter Froning a,*, Junliang Yu a, Gerd Gaiselmann b, Uwe Reimer a, Ingo Manke c, Volker Schmidt b, Werner Lehnert a, d

a Forschungszentrum Jülich GmbH, Institute of Energy and Climate Research, IEK-3: Electrochemical Process Engineering, D-52425 Jülich, Germany
b Institute of Stochastics, Ulm University, Germany
c Helmholtz-Zentrum Berlin GmbH, Institute of Applied Materials, D-14109 Berlin, Germany
d Modeling in Electrochemical Process Engineering, RWTH Aachen University, Germany

Abstract

Gas transport in non-woven gas diffusion layers of a high-temperature polymer electrolyte fuel cell was calculated with the Lattice Boltzmann method. The underlying micro structure was taken from two sources. A real micro structure was analyzed in the synchrotron under the impact of a compression mask mimicking the channel/rib structure of a flow field. Furthermore a stochastic geometry model based on synchrotron X-ray tomography studies was applied. The effect of compression is included in the stochastic model. Gas transport in these micro structures was simulated and the impact of compression was analyzed. Fiber bundles overlaying the micro structure were identified which affect the homogeneity of the gas flow. There are significant deviations between the impact of compression on effective material properties for this type of gas diffusion layers and the Kozeny-Carman equation.

© 2016 Elsevier B.V. All rights reserved.

1. Introduction

The knowledge of the characteristics of polymer electrolyte fuel cell (PEFC) components is essential for the efficient operation of fuel cells and stacks. It can be supported by mass transport simulations at different spatial scales. The gas flow is often affected by material properties of the components. Gas diffusion layers (GDL) are used in low temperature PEFCs as well as in high temperature PEFCs (HT-PEFC) in order to distribute gases from the channels under the ribs of the flow field and collect the product gas on the cathode side. The transport characteristics of the GDL depend highly on the micro structure of the material which is of stochastic nature and can furthermore change under mechanical
compression. In former times, the effect of GDL was typically neglected in three dimensional (3D) cell and stack simulations [1]. But with increasing computational power the effect of GDL properties is often included [2], Research groups are working on several fields covering the micro structure of the material and its characterization regarding mass transport and its impact on fuel cell applications. Experimental work and modeling of GDL complement one another in the development of PEFC and HT-PEFC. At this point, modeling of the micro structure [3–5] is often complemented by transport simulations. The micro structure of the material needs to be detected and transformed into geometry information to be used by the simulation software. The impact of transport characteristics on the fuel cell operation is of considerable evidence for the design of improved materials.

Experimental studies can follow various approaches. The permeability of GDLS was measured by Feser et al. [6] and also by Hussaini and Wang [7]. Taira and Liu [8] measured the effective permeability of GDL under the land region of a flow field. The general agreement of commonly used equations for permeability and tortuosity with visualizations of the micro structure of GDL was shown by Fishman and Bazylik [5]. The permeability of porous materials can be related to geometric properties for certain materials as shown by Tamayo et al. [9] and Hossain et al. [10] in their investigations on single phase gas transport in GDL. Several groups investigated liquid water distribution in operating PEFCs with neutron [12–14] and synchrotron X-ray imaging [15,16]. Experimental studies on the effect of compression on the performance of a PEFC were presented by Lee et al. [17]. Another kind of experiments was presented by Ye et al. [18] who investigated the bypass of water under the rib between two parallel gas flow channels. The GDL in their experiments was compressed by applying a defined tension to the flow field. A link between the micro structure of porous materials and its transport properties was presented by Koponen et al. [19]. Effective properties as permeability and tortuosity can be calculated from the flow fields resulting from Lattice Boltzmann (LB) simulations. This work bridges experimental work and simulations on both micro structures and cell level.

Various research groups are working on transport simulations in the micro structure of GDLS. Matyka et al. [20] calculated the tortuosity from streamlines which were obtained from two-dimensional LB simulations in randomly constructed porous structures. Thomas et al. [21] determined the accuracy of such results in relationship to the spatial discretization of the micro structure. Espinoza et al. [22] investigated the effect of compressed GDL on the permeability and tortuosity of a GDL with two-dimensional LB simulations. Gao et al. [23] focused on liquid water transport in GDL micro structures using three-dimensional LB simulations. Paper-type GDLS were reconstructed by Daino and Kandlikar [24] under consideration of the distribution of polytetrafluoroethylene (PTFE) in the micro structure. Another stochastic geometry model [25] was taken by Froning et al. [26] to determine permeability and tortuosity of paper-type GDL represented by evaluating transport simulations in the micro structure. Through-plane and in-plane transport simulations using the Lattice Boltzmann method (LBM) were performed in micro structures under different levels of compression up to 50%. Nabovati et al. [27] calculated through-plane and in-plane permeability and tortuosity of reconstructed paper-type GDL using LB simulations. Under different conditions regarding homogeneous and heterogeneous porosity distributions they found higher in-plane permeabilities and lower in-plane tortuosities than the through-plane counterparts. Another kind of GDLS uses non-woven fleece, also made of carbon fibers. Su et al. [28,29] use this type of GDL in their investigations on polymer binder and platinum distribution in catalyst layers. Non-woven fiber based materials can have a more complex micro structure which is also available for stochastic modeling. Gaiselmann et al. [30,31] investigated non-woven GDL from Freudenberg. They identified fiber bundles as superposed structures and incorporated them as a feature of their stochastic geometry model. Rama et al. [32] simulated gas transport in GDLS with the LBM in three-dimensional micro structures of woven carbon-cloth GDL from reconstructed X-ray micro-tomography which were compressed by applying dedicated weights to the GDL structure. They calculated pore sizes, porosity, permeability and tortuosity of woven GDLS under varying grades of compression. The anisotropy of the GDL as a function of compression was also presented.

Effective transport properties obtained from measurements or micro scale simulations can be used as model parameters in higher spatial scales. The presence of liquid water at low temperatures leads to different dominating effects for PEFC and HT-PEFC. In particular, Chippar et al. [33] studied the effect of GDL compression in PEFCs. They considered the impact of compression on effective transport properties of the GDL and the water saturation. Ju [34] studied the effect of anisotropy of the GDL on heat and water transport in a fuel cell. He investigated the anisotropy of the current density under the channel and under the rib crossings to the flow direction of a 0.5 mm wide channel. Hossain et al. [35] investigated the effect of GDL permeabilities on the efficiency of PEFC using a two-phase model. They observed high deterioration of the performance of a PEFC at low in-plane permeability of the GDL. Qi et al. [36] calculated the deformation of the GDL of a PEFC under mechanical compression. Bosomoi et al. [37] investigated effective transport properties of fresh and aged GDL also under the land and channel regions of a flow field of a HT-PEFC. Chippar and Ju [38,39] modelled the gas crossover through the MEA of a HT-PEFC between a pair of fuel and gas channels of 1 mm width. The relevance of their investigations is affirmed by HT-PEFC stacks when they are assembled with meander type flow fields. Lüke et al. [40] measured the inhomogeneity of the current density distribution in a HT-PEFC stack with meander flow fields operated under several conditions.

In our paper we simulated gas transport in the micro structure of a GDL. The investigation was motivated by the research of Lüke et al. [40] and Kvesić and Kvesić [41]. Their experiments on HT-PEFC stacks and corresponding Computational Fluid Dynamics (CFD) simulations showed the evidence of in-plane gas transport under the ribs of meander type flow fields. Liu et al. [42] presented a HT-PEFC with spiral flow fields which also benefits from in-plane gas transport under the ribs. To get insight into the underlying processes the micro structure of a Freudenberg GDL of type H2315 was investigated in the BESSY synchrotron by Tötzke et al. [43]. From this micro structure a stochastic geometry model of the GDL was developed [44]. The geometry model can generate stochastic equivalent geometries of the uncompressed and compressed micro structure. Furthermore, the real micro structure was investigated in the BESSY synchrotron under the impact of compression by the ribs of the flow field on the micro structure. Transport simulations in these geometries were performed using the LBM. The effective transport properties permeability and tortuosity calculated from the results were analyzed. This numbers can be used for investigations of transport processes on cell and stack level [2,34,41]. Furthermore the inhomogeneous transport of gases under the ribs of the flow field was evaluated.

2. Methods

The micro structure of Freudenberg GDL (type H2315) was investigated in the BESSY synchrotron. The material was compressed virtually and also by a mechanical device according to Fig. 1 which depicts the processes of our investigations. Combining
elements in our study of different GDL samples are the detection of
the micro structure and transport simulations. Gas transport was
simulated with the LBM and evaluated for material characterization
and to locate inhomogeneities.

2.1. Detection of micro structure

Two GDL samples were investigated in the BESSY synchrotron.
Sample I was used as a basis for the development of a geometry
model of the micro structure. This is no. O in Table 1.

The three-dimensional data of the compressed material was
used to generate a stochastic model of the micro structure as pre-
sented by Gaiselmann et al. [30]. Six realizations were created ac-

Fig. 1. Experimental and simulation scheme.

Table 1
Uncompressed original micro structure (O), realizations of stochastic geometries (A-
F) and real geometries under the rib (L, R; footprints in Fig. 3). The porosity is
specified for the uncompressed material. X denotes available geometries.

<table>
<thead>
<tr>
<th>GDL sample</th>
<th>No</th>
<th>Porosity /%</th>
<th>Compression /%</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>0 10 20 30 40 50 60 70</td>
<td></td>
</tr>
<tr>
<td>I</td>
<td>O</td>
<td>76.5 X</td>
<td></td>
</tr>
<tr>
<td></td>
<td>A</td>
<td>76.4 X X</td>
<td></td>
</tr>
<tr>
<td></td>
<td>B</td>
<td>76.1 X X</td>
<td></td>
</tr>
<tr>
<td></td>
<td>C</td>
<td>76.7 X X</td>
<td></td>
</tr>
<tr>
<td></td>
<td>D</td>
<td>76.1 X X</td>
<td></td>
</tr>
<tr>
<td></td>
<td>E</td>
<td>76.3 X</td>
<td></td>
</tr>
<tr>
<td></td>
<td>F</td>
<td>76.5 X X X X</td>
<td></td>
</tr>
<tr>
<td>II</td>
<td>L</td>
<td>77.0 X X X X</td>
<td></td>
</tr>
<tr>
<td></td>
<td>R</td>
<td>77.0 X X X X</td>
<td></td>
</tr>
</tbody>
</table>

Fig. 2 shows a layer in the original structure and in a realization of
the stochastic model. The images of size 1500 by 1500 build a
section of 1.25 by 1.25 mm² (Fig. 2). Every series of images contains
of 240 layers representing a GDL thickness of 200 μm for the un-
compressed material. The representation of the 70% compressed
material still contains 72 images.

The GDL has a superposed structure built from fiber bundles
which are considered by the stochastic model of the geometry.
While the bundles cross the GDL plane in arbitrary direction they
are favored in coordinate direction by the stochastic model. This
can be seen in the upper left region of the right image in Fig. 2.
The horizontal line is part of a fiber bundle which makes the modelled
geometry stochastic equivalent to the real structure but it looks
different at local positions. The fiber bundles build a superstructure
with spatial dimensions in millimeter scale.

Sample II was compressed using a mechanical device introduced
by Tötzke et al. [43]. The compression device contained a mask with a
channel/rib structure to represent the situation under the flow
field of a fuel cell. Fig. 3 shows pieces of the real micro structure
obtained from the BESSY synchrotron.

The images in Fig. 3 were taken from the gray level images from
the synchrotron and converted into black/white images. The voxel
size of the synchrotron images defined the spatial scale of the
transport simulations. In this way every image is representing a
layer of the GDL of 0.876 μm thickness. The images of size 2000 by
2000 show a GDL section of 1.75 by 1.75 mm². Images close to the
sample holder of the compression device show artifacts due to the
manufacturing tolerance. Therefore a layer as close as possible to
the sample holder was chosen as the basis layer. The chosen layer
0 (Fig. 3(a)) still shows some hint on the artifacts in the omitted
images but it is dominated by the GDL structure as shown in the
series of images in Fig. 3 which show the layers 0, 5, 10, and 15 steps
of 0.876 μm towards the GDL structure. They show GDL micro
structures which are not affected by external macro structures. But
in this layers fiber bundles are hidden which are laid throughout
the GDL micro structure similar as those from the other sample
shown in Fig. 2. For the uncompressed case 268 images were
available for the channel/rib scenario: layers 0 to 267. This includes
50 images where the GDL intrudes into the channel region. In the
simulations of gas transport from the channel to the closed end of
the structure the gas inlet is at layer 267, and layer 0 is the bottom
layer at the GDL exit. At 10% compression 240 images were avail-
able, 224 images for 20% compression, and for 30% compression
there were 197 images available for the channel/rib scenario. For
the simulations on material characterization the section under the
ribs were extracted — red frames in Fig. 3. Furthermore approx. 20
images were left out from the bottom of the images stack. In Fig. 3,
the images (a) to (c) look more irregular than image (d). Therefore
only 248 images were selected in the uncompressed case, 222 for
10% compression, 205 for 20% compression and 178 images were
selected for the 30% compressed case.

2.2. Numerical transport simulations

The gas flow in the micro structure was simulated using the
Lattice Boltzmann method. The open source software Palabos [45]
was used with the BGK scheme and the D3Q19 discretization
[46–48]. Three groups of transport simulations were run.

1. Effective transport properties were evaluated from transport
simulations in real and stochastic geometries of sample I. This is
according to lines 0 and A to F in Table 1.

2. The GDL under the ribs of the real structure from sample II was
examined for effective transport properties. This is represented
by lines L and R in Table 1.
3. The gas transport under the rib of a flow field of sample II was investigated on real compressed GDL.

For the evaluation of effective transport properties of the stochastic geometries from Table 1, lines A-F, transport simulations were run similar as presented in Ref. [49]. Fig. 2 shows clearly that the stochastic geometry is not showing the real geometry exactly but it builds a micro structure which is equivalent to the real structure under stochastic view.

Like in previous studies [26,49], an empty space of 20 layers was added upstream and downstream to allow the definition of standard boundary conditions at the inlet and outlet without interfering with the irregular micro structure of the GDL. Inlet conditions were chosen with fixed velocity which was calculated from the total amount of hydrogen to be converted via Faraday’s law under the assumption of a mean current density of 1 A cm$^{-2}$ – also known as Dirichlet boundary condition. At the outlet, constant pressure was assumed which is known as a Neumann boundary condition. At the four sides of the simulation domain wall boundary conditions were specified. The simulations were performed through-plane and in-plane. The in-plane simulations were run in two directions because the construction process of the GDL does not allow the assumption of properties being independent from the flow direction. Fig. 4 shows the simulation frame around a series of black/white images specifying the underlying micro structure. The annotation in the diagram is according to the through-plane situation.

Effective transport properties were also evaluated in real structures (sample II). For this purpose the compressed sections under the rib were extracted for transport simulations (Table 1, lines L, R). This regions were extracted as 550 by 2000 sections from the left (L) and right (R) side of each of the original 2000 by 2000 images.

For the evaluation of effective transport properties the transport was simulated in through-plane ($x$) direction and in two perpendicular in-plane directions ($y, z$). Because of superposed structures it cannot be assumed that the micro structure has isotropic in-plane conditions even under stochastic view [30,43].

Local behavior of the gas flow in the compressed micro structure of sample II was investigated by transport simulations in the real structure. The micro structure is represented by images of size 2000 by 2000, each voxel of size 0.876 $\mu$m. With this image series a section of 1.75 by 1.75 mm$^2$ is represented. The width of the channel structure is 890 pixels according to 780 $\mu$m (Fig. 3). This is a finer resolution than for sample I. According to Thomas et al. [21] a more accurate calculation of the pressure can be possible as long as other essential parameters do not change.

3. Results

3.1. Effective transport properties

Effective properties of the material were extracted from the simulation results of the homogeneous compressed real and stochastic geometries from Table 1, lines A-F. Similar as done in Ref. [26] the permeability $\kappa$ was calculated from the velocity field via Darcy’s law

$$\kappa = -\frac{q \cdot \mu}{\nabla P} \quad (1)$$

In this equation $q$ is the flux through the porous structure, and $\mu$ is the dynamic viscosity of the gas. $\nabla P$ is the pressure drop between the entry layer where the gas enters the GDL and the exit layer where the gas leaves it. The reciprocal value of $\kappa$ can be used as a flow resistivity by porous media sub-models in CFD software. Kvesić et al. [41] used this approach with the ANSYS/Fluent software. Cao et al. [50], and Beale [51] used the same method for their CFD simulations of HT-PEFC with the open source software OpenFOAM. The tortuosity $\tau$ can be approximated by the approach according Koponen et al. [19].

$$\tau = \frac{<|v|>}{<v_x>} \quad (2)$$

Eq. (2) allows the calculation of the tortuosity from the velocity field of the transport simulation. $|v|$ is the absolute value of the velocity and $v_x$ is its component in flow direction. $< >$ denotes the spatial average over the region of interest, the GDL in our simulations. Eq. (2) was proven to be correct for capillary systems [19].

The tortuosity and permeability were also calculated in three directions of the real structure from under the rib in the channel/rib
scenario. In Table 1 this geometries are specified as L and R, denoting the left and right ribs.

The calculated effective values for permeability and tortuosity are shown in Table 2. In any cases the in-plane permeability in at least one of the two in-plane directions is approx. 50% higher than the through-plane permeability which is shown in the rightmost two columns where the in-plane permeabilities $k_1$ and $k_2$ were divided by the through-plane permeability $k_0$. This characteristic promotes the gas flow under the ribs of the flow field. This is in agreement with our previous results on paper-type GDL [26] and with the results of Nabovati et al. [27] who found the same tendency regarding in-plane and through-plane characteristics. The difference is that the in-plane characteristics of paper-type GDLs are independent from the in-plane direction per definitionem. The stochastic geometry model from Gaiselmann et al. [30] was fitted to 3D synchrotron data of the micro structure. It incorporates anisotropy of the in-plane properties of the GDL. The absolute permeability decreases under compression.

The most prominent property in Table 2 is the effective permeability which is depicted in Fig. 5(a). It shows results from simulations in real geometries from samples I and II and from realizations of the stochastic model from sample I. The through-plane permeability $k_0$ and the in-plane permeabilities $k_{1,2}$ were given the same color for both samples I and II according to their directions. The vertical bars show the minimum and maximum values where they are available. For sample I, the largest difference in the min/max values are for $k_1$ which is the in-plane permeability in the direction of the modelled fiber bundles. The GDL section analyzed in the synchrotron was not aligned to the orientation of the fiber bundles. Therefore the in-plane properties of the original data of sample I — entry O in Table 2 — are not aligned with those of the realizations A-F of the stochastic model. When in-plane characteristics become dominant for an application the MEA possibly might be assembled using a GDL rotated according to the orientation of the fiber bundles. For sample II the permeabilities in in-plane directions are not clearly separated according to their orientation because the coordinates of the simulation domain are not aligned with the orientation of the fiber bundles. The highest difference in the min/max values of the in-plane permeability is for $k_1$ which is the direction of the shorter extent of the simulation domain (across the channel). Because of the domain size which is in the order of magnitude of the fiber bundles the behavior of the permeability is completely different from sample I.

It can be stated that the permeability values of the real geometry (L, R) differ from those of the stochastic geometries (A-F). The simulations on stochastic geometries show significant differences in the in-plane permeabilities $k_1$ and $k_2$ in the two directions along the coordinate axes. The reason is a superposed structure in the GDL material caused by the manufacture which can be seen in Fig. 3, layers 5 to 15. It shows that bundles of fibers are oriented approx. 30° skew to the top-down direction. This structure can also be observed in the resulting velocity profile in Fig. 7. The fiber bundles are considered by the stochastic model of the geometry in the coordinate directions [30]. Therefore the impact of the fiber bundles on the material properties is pronounced by simulations on the stochastic geometries. In the real geometries (O, L, R) the fiber bundles are not oriented along coordinate axes. Therefore the in-plane transport properties $\kappa$ and $\tau$ cannot be compared to those of the cases A-F. Moreover, the impact of the orientation of the fiber bundles on in-plane transport properties is smeared in simulations on the real geometry.

Like in our former investigations on another type of compressed GDL [26], we validated the transport simulations in the compressed micro structures according to the Kozeny-Carman trend. The permeability $\kappa$ of a porous structure can be estimated from geometric properties by the Kozeny-Carman equation

$$\kappa = \frac{e}{K_c} \left( \frac{V_p}{S_p} \right)^2 .$$

(3)

The geometric properties in Eq. (3) are the porosity $e$, the total volume $V_p$ and the inner surface $S_p$. Tomadakis and Robertson [52] showed that the Kozeny constant $K_c$ is related to the tortuosity $\tau$

$$K_c = \tau \cdot K_c$$

(4)

with $K_c$ depending only of the shape of the micro structure. Both equations lead to

$$\kappa \cdot \tau \sim e \left( \frac{V_p}{S_p} \right)^2 .$$

(5)

Tötzke et al. [43] stated that in case of homogeneous compression the fibers are mainly translated in through-plane direction. Supposed the shape of the micro structure does not change under compression, Eq. (5) can be used to estimate the term $\kappa \cdot \tau$ of compressed material based on its known value of uncompressed material via

$$\kappa \cdot \tau |_{\text{Ko}} = \kappa \cdot \tau |_{\text{Ko}} \cdot e \left( \frac{V_p}{S_p} \right)^2 |_{\text{Ko}} / e \left( \frac{V_p}{S_p} \right)^2 |_{\text{K}} .$$

(6)

In Eq. (6) the notation $|_{\text{Ko}}$ specifies properties of the uncompressed material and $|_{\text{K}}$ denotes material with $x\%$ compression. Analyzing Eq. (6) leads to general expectations on the impact of $\kappa \cdot \tau$ under compression. While the volume $V_p$ is reduced under compression the inner surface $S_p$ should not change much under the assumption that the shape of the micro structure is kept. The total volume $V_p$ decreases and also does the porosity $e$ as long as it is much larger than the compression. Then $\kappa \cdot \tau$ must decrease.

The simulated $\kappa \cdot \tau$ is shown in Fig. 5(b). The deviation of the simulated value from the Kozeny-Carman (KC) trend is summarized in Table 3.

The Kozeny-Carman trend $\kappa \cdot \tau |_{\text{Ko}}$ (Fig. 5(b)) of the stochastic geometries A-F of the compressed Freudenberg GDL decreases with
Moreover, the through-plane Eq. (6). Especially for the L case the simulated values but the shape of the curve looks concave. The deviation of $k$ in Ref. [26] up to 40% compression which is the range of practical compression and the curve has a convex shape. It shows the evidence of the stochastic geometries.

In Figs. 3 and 6 it is shown how the simulation domain of the stochastic geometries. Furthermore the superstructure built by the fiber bundles has similar spatial dimensions as the channel width. This shows the evidence of the size of the simulation domain for material characterization in presence of overlaid structures.

### Table 2

<table>
<thead>
<tr>
<th>No.</th>
<th>Compression/ %</th>
<th>Through-plane</th>
<th>In-plane 1</th>
<th>In-plane 2</th>
<th>$k_{1/k_0}$</th>
<th>$k_{2/k_0}$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>$\tau$</td>
<td>$k_{0},\mu$m$^2$</td>
<td>$\tau$</td>
<td>$k_{1},\mu$m$^2$</td>
<td>$\tau$</td>
</tr>
<tr>
<td>O</td>
<td>0</td>
<td>1.207</td>
<td>6.67</td>
<td>1.158</td>
<td>9.74</td>
<td>1.149</td>
</tr>
<tr>
<td>A</td>
<td>0</td>
<td>1.208</td>
<td>10.85</td>
<td>1.138</td>
<td>15.64</td>
<td>1.170</td>
</tr>
<tr>
<td>B</td>
<td>10</td>
<td>1.219</td>
<td>6.30</td>
<td>1.252</td>
<td>5.92</td>
<td>1.72</td>
</tr>
<tr>
<td>C</td>
<td>20</td>
<td>1.235</td>
<td>6.83</td>
<td>1.110</td>
<td>10.71</td>
<td>1.180</td>
</tr>
<tr>
<td>D</td>
<td>30</td>
<td>1.241</td>
<td>7.67</td>
<td>1.105</td>
<td>11.52</td>
<td>1.180</td>
</tr>
<tr>
<td>E</td>
<td>40</td>
<td>1.249</td>
<td>7.62</td>
<td>1.103</td>
<td>9.76</td>
<td>1.363</td>
</tr>
<tr>
<td>F</td>
<td>50</td>
<td>1.264</td>
<td>7.62</td>
<td>1.110</td>
<td>10.71</td>
<td>1.180</td>
</tr>
<tr>
<td>G</td>
<td>60</td>
<td>1.272</td>
<td>5.86</td>
<td>1.117</td>
<td>8.48</td>
<td>1.161</td>
</tr>
</tbody>
</table>

The situation for the values of sample II looks similar in Fig. 5(b) on the first view. The Kozeny-Carmen trend is close to the $k-\tau$ values but the shape of the curve looks concave. The deviation of the simulated $k-\tau$ values from the sections under the rib of sample II (L, R) is larger — especially for small amounts of compression. Moreover, the through-plane $k-\tau$ does not behave as expected from Eq. (6). Especially for the L case $k-\tau$ is even increasing from 0 to 10% compression. The simulations were run on sections 550 by 2000 which ranges from the outer border to the edge under the rib of the flow field. In Figs. 3 and 6 it is shown how the simulation domain of the L, R cases is specified by the footprint of the ribs. As the fiber bundles are crossing the edge of the rib the pre-condition of the Kozeny-Carman equation — the same shape of the uncompressed and the compressed geometry — may possibly be violated. That may be a reason why the entries in lines L and R of Table 3 show a different trend as the stochastic geometries. Furthermore the superstructure built by the fiber bundles has similar spatial dimensions as the channel width. This shows the evidence of the size of the simulation domain for material characterization in presence of overlaid structures.

#### 3.2. Channel/rib scenario

The simulation of the gas transport in the channel/rib scenario (sample II) was evaluated under the viewpoint of inhomogeneous mass transport. The results of the through-plane simulations in the channel/rib scenario were evaluated locally at the layer where the gas exits the GDL. Fig. 6 shows the through-plane component of the velocity field at the position where the gas leaves the GDL. Rightmost to the label ‘1’ in the image there is a dark blue circle which coincides with a circular artifact shown in layer 0 of Fig. 3(a). The fibers left and right to the label ‘2’ can be seen in layers 5 and 10 (Fig. 3(b),(c)) but not in layer 0. Hence, the lines in Fig. 6 are shadows of the real fibers nearby. The fiber right to the three labels ‘3’ can be seen in layer 0 whereas the two lines nearby the two labels ‘4’ are shadows of the fibers in layer 5 (Fig. 3(b)). The velocity field from Fig. 6 is evaluated with statistical methods. The x coordinate of the transport simulations is the through-plane direction. The y coordinate is across the channel, the z coordinate is along. The position across the channel is treated as independent stochastic variable. Every horizontal line was interpreted as a realization of gas transport in the stochastic material along the x coordinate, denoted as entities in Fig. 6. The velocity field in this layer looks
irregular on every compression level which is demonstrated by Fig. 7. This series of images show the situation of the gas flow at the position where the gas leaves the GDL. The image in Fig. 6 shows a section of 1.75 by 1.75 mm² with a 0.8 mm wide channel in the middle, and two ribs on the left and right side. The scale of the velocity in Fig. 6 ranges from 0 to 1.4 $\times 10^{-4}$ m s⁻¹. It is colored from blue (low) via white to red color (high). The fibers at this position are shown as dark blue shadows. They do not change under compression because the bottom level is fixed in the experimental setup. Fig. 7 enlarges the region marked by the white frame in Fig. 6. Fig. 7 shows (a) the uncompressed situation, and the situation under 10, 20, and 30% compression ((b), (c), (d)). The fibers at the bottom are visible on every image. With increasing compression fiber layers which were only visible as shadows under 0% compression come into the foreground. Furthermore, a separation of the velocity into bright and dark regions evolve under the edge of the rib. From left to right the brightness region left from the rib footprint increases while the colors at the right part under the rib become a little bit darker. But this effect has to be noted with care because this images represent only a very small region of the whole simulation domain.

A significant information in the channel/rib scenario is the amount of gas being transported under the rib of the flow field. For this purpose the resulting velocity field in the post processing layer is analyzed one-dimensional in y direction which is the abscissa in Fig. 6. The ordinate in the same diagram represents the entities measured at the y position across the channel. The entities are the number of observations which is the number of horizontal lines in the images of Figs. 6 and 7 in this case. They are weighted by the through-plane velocity of the gas in transport (x) direction. The velocities in the yz plane at the GDL exit are evaluated along the y coordinate as statistical density weighted by the velocity. This method simplifies the flow in the sense that winding paths of the real flow lines in the three dimensional micro structure – e. g., in order to flow around fibers – are neglected in y direction. To get statistical densities the weighted values need to be normalized because the integral must be equal to one. In particular, densities $d_k$, $k$ denoting the grade of compression, can be calculated by the following approach.

<table>
<thead>
<tr>
<th>Compression / %</th>
<th>A</th>
<th>B</th>
<th>C</th>
<th>D</th>
<th>E</th>
<th>F</th>
<th>L</th>
<th>R</th>
</tr>
</thead>
<tbody>
<tr>
<td>10</td>
<td>6.9</td>
<td>12.9</td>
<td>8.6</td>
<td>10.9</td>
<td>10.3</td>
<td>0.1</td>
<td>1.13</td>
<td>13.2</td>
</tr>
<tr>
<td>20</td>
<td>6.9</td>
<td>12.9</td>
<td>8.6</td>
<td>10.9</td>
<td>10.3</td>
<td>0.1</td>
<td>1.13</td>
<td>13.2</td>
</tr>
<tr>
<td>30</td>
<td>6.9</td>
<td>12.9</td>
<td>8.6</td>
<td>10.9</td>
<td>10.3</td>
<td>0.1</td>
<td>1.13</td>
<td>13.2</td>
</tr>
<tr>
<td>40</td>
<td>6.9</td>
<td>12.9</td>
<td>8.6</td>
<td>10.9</td>
<td>10.3</td>
<td>0.1</td>
<td>1.13</td>
<td>13.2</td>
</tr>
<tr>
<td>50</td>
<td>6.9</td>
<td>12.9</td>
<td>8.6</td>
<td>10.9</td>
<td>10.3</td>
<td>0.1</td>
<td>1.13</td>
<td>13.2</td>
</tr>
<tr>
<td>60</td>
<td>6.9</td>
<td>12.9</td>
<td>8.6</td>
<td>10.9</td>
<td>10.3</td>
<td>0.1</td>
<td>1.13</td>
<td>13.2</td>
</tr>
<tr>
<td>70</td>
<td>6.9</td>
<td>12.9</td>
<td>8.6</td>
<td>10.9</td>
<td>10.3</td>
<td>0.1</td>
<td>1.13</td>
<td>13.2</td>
</tr>
</tbody>
</table>

Fig. 5. (a) Effective permeability of the GDL samples. $k_{\|}$ through-plane direction, $k_{\perp}$ in-plane directions. Filled symbols: real geometries of samples I and II; outlined symbols: stochastic realizations of sample I. (b) Comparison of $k_{\|}$ from transport simulations with the KC trend (Eq. (6)).
\[ d_k(y) = \int v_k(y,z) \, dz \]  

(7)

at the position \( y \) across the channel, velocity components \( v_k \) in transport direction, \( z \) being the along-the-channel direction. Weights \( w_k \) are chosen to ensure that \( \int w_k \cdot d_k(y) \, dy = 1 \) which makes the function \( w_k \cdot d_k \) a statistical density. The resulting relative densities

\[ d_k(y) = w_k \cdot d_k(y) / \bar{w}_k \cdot \bar{d}_k \]  

(8)

can be interpreted as relative velocities at a particular position across the channel as shown in Fig. 8. The average value of \( \bar{d}_k \) is 1. The diagram shows a large variation in the velocity field across the channel. Though the variation across the channel is larger than the deviation between the curves a systematic impact of the compression can be stated. It is shown that the variation of the velocity across the channel does not change with compression since it is caused by the irregular micro structure. The velocity in the area under the channel is higher with increasing compression.

The situation under the rib is reverse: the velocity decreases under compression. Stochastic evaluations of the flow field in the channel/rib scenario were performed with the R package [53].

From the one-dimensional density (Fig. 8) it can be calculated how much gas is transported under the ribs of the flow field structure. This can be done by evaluating the cumulated sum of the density shown in Fig. 8. The result in percentage is shown in Table 4.

The table shows that the transport of gases under the ribs is inhibited by the compression of the GDL caused from the ribs of the flow field. The mass transport under the left and the right rib is possibly affected by the superposed structure of the fiber bundles which is of similar size as the footprints of the ribs in our simulations.

4. Conclusion

Within this work the gas transport in non-woven type GDLs was simulated by using the Lattice-Boltzmann method. The geometric information was taken from three sources: 1) a real micro structure obtained from X-ray tomography, 2) a stochastic geometry model that allows for multiple generation of samples which are stochastically equivalent (i.e., from the same material), and 3) a real geometry of a channel/rib construction. The region under the rib was cut out for material characterization. The transport properties of uncompressed and compressed material were studied in view of effective permeability \( \kappa \) and tortuosity \( \tau \), both of them calculated from through-plane and in-plane transport simulations. The in-plane permeability is higher than the through-plane permeability in all cases. This information is useful in CFD simulations supporting the flow field design of HT-PEFC stacks.

For compressed material the impact of compression on the product of the permeability and the tortuosity \( \kappa \cdot \tau \) was evaluated in order to check the consistency of the simulation results. The trend which is expected according to the Kozeny-Carman equation could not be confirmed for this kind of non-woven GDLs. One possible explanation is the fact that the underlying super-structure of fiber bundles is on the same length scale as the size of the modeling domain of the smaller GDL sample.

A channel/rib scenario representing a repeating unit of the target application was analyzed qualitatively. The transport of gas under the ribs of the flow field is inhibited by the compressed micro structure of the GDL. Irregularities were found across the gas channel – possibly due to the superposed structure. For this kind of micro structure the impact of overlaid fiber bundles on the gas flow is larger than the impact of mechanical compression. This confirms the conclusion above that for material characterization the cross section of the simulation domain should be larger than the extent of relevant structures.

<table>
<thead>
<tr>
<th>Compression %</th>
<th>Mass transfer under the ribs/%</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Left</td>
</tr>
<tr>
<td>0</td>
<td>5.7</td>
</tr>
<tr>
<td>10</td>
<td>4.4</td>
</tr>
<tr>
<td>20</td>
<td>3.8</td>
</tr>
<tr>
<td>30</td>
<td>2.6</td>
</tr>
</tbody>
</table>

Fig. 7. Sample II: Through-plane velocity in a 500 \( \times \) 500 section of the GDL exit layer. (a) Uncompressed, (b) 10% compression, (c) 20% compression, (d) 30% compression. GDL section of size 0.44 by 0.44 mm\(^2\). Footprint of the rib in red. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

Fig. 8. Sample II: Density of the through-plane velocity at the GDL exit layer.