



Measuring the Effectiveness of a Test

(Converting Software Testing from an Art to a Science)

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Abstract: The proposed paper presents a set of metrics developed by the author while working as a test consultant for a Viennese software house from 1998 until 2003. They were intended to be used to measure the performance of the test department there, but they are equally valid for measuring test operations anywhere. In fact, with these metrics it should be possible to convert software testing from an art as perceived by Glenford Meyers in 1975 to a science as defined by Lord Kelvin in 1875. The metrics were obtained using the Goal/Question/Metric Method of Basili and Rombach and were refined through many years of practical application. They are supported by a set of tools designed for both static and dynamic analysis as well as for evaluating the results of both.

Keywords: *Test Management, Test Objectives, Defect Analysis, Test Coverage, Software Metrics, Test Metrics.*

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Lord Kelvin on Measurement

„When you can measure what you are speaking about, and express it in numbers, you know something about it, but when you cannot measure it, when you can not express it in numbers, then your knowledge is of a meagure and unsatisfactory kind.“

from Lord Kelvin

British physicist, 1882

Tom DeMarco on Measurement

„You can not control what you can not measure. Measurement is the prerequisite to management control. “

from Tom DeMarco
American Consultant, 1982

Test Metric Categories

- Metrics for assessing the testability of the software
- Metrics for evaluating test cases
- Metrics for calculating test costs
- Metrics for measuring test coverage
- Metrics for assessing test effectiveness

Testability at the Unit Test Level

- Unit Complexity = Size * Cohesion * Coupling
- Control path complexity = Control flow branches / Statements
- Interface complexity = Interfaces + Parameters / Statements
- Data complexity = Conditional variables / Variables used
- Unit Testability = 1 - Average
(Unit-Complexity, Control-Flow-Complexity, Interface-Complexity, Data-Complexity)

Testability at the Integration Test Level

- Interface volume = $\frac{\text{Interfaces}}{\text{Interfaces} + \text{Components}}$
- Interface complexity = $\frac{\text{Parameters}}{\text{Parameters} + \text{Interfaces}}$
- Database access frequency = $\frac{\text{Components without Database accesses}}{\text{Components}}$
- Interface Visibility = $\frac{\text{invisible Interfaces}}{\text{Interfaces}}$
- Integration Testability = $1 - \text{Average}$
(Interface-Volume, Interface-Complexity, Database-Access Frequency, Interface-Visibility)

Testability at the System Test Level

- User Interface Volume = $\frac{\text{User Interfaces} + \text{Controls}}{\text{System Variables}}$
- System Interface Volume = $\frac{\text{System Interfaces} + \text{Data Elements}}{\text{System Variables}}$
- Database Volume = $\frac{\text{Tables} + \text{Attributes}}{\text{System Variables}}$
- UseCase Volume = $\frac{\text{UseCases}}{\text{System Functions}}$
- System Testability = $1 - \text{Average}$
(User-Interface-Volume, System-Interface-Volume, Database-Volume, UseCase-Volume)

Measuring the Complexity of Test Cases

- Test data complexity = test data types / test data instances
- Test data density = test control variables / test data
- Test case volume = $1 - (\text{test cases} / \text{test data instances})$
- Test case intensity = $1 - (\text{use cases} / \text{test cases})$
- Test case complexity = Average (Test data complexity, Test data density, Test case volume, Test case intensity)

Measuring the Quality of Test Cases

- Test case impact = $1 - (\text{test cases} / \text{impacted functions})$
- Test case reusability = $(\text{automated test cases} / \text{test cases})$
- Test case conformity = $(\text{formally correct test case attributes} / \text{total test case attributes})$
- Test case affectivity = $(\text{weighted errors detected} / \text{test cases executed})$
- Test case quality = Average
(Test case impact, test case reusability, test case conformity, test case affectivity)

Test Case Analysis Report for FIVS

| | | | |
|-----------|----------|------------------------|-------|
| Module: | GWMBRACO | Number of Test Cases = | 106 |
| Module: | GWMDERIV | Number of Test Cases = | 761 |
| Module: | GWMEMIBE | Number of Test Cases = | 128 |
| Module: | GWMEMISS | Number of Test Cases = | 325 |
| Module: | GWMEXDAT | Number of Test Cases = | 167 |
| Module: | GWMFETAG | Number of Test Cases = | 139 |
| Module: | GWMFI | Number of Test Cases = | 3070 |
| Module: | GWMFIBEZ | Number of Test Cases = | 880 |
| Module: | GWMFIKAT | Number of Test Cases = | 597 |
| Module: | GWMFIKNU | Number of Test Cases = | 341 |
| Module: | GWMIDENT | Number of Test Cases = | 886 |
| Module: | GWMINDX | Number of Test Cases = | 838 |
| Module: | GWMINSKA | Number of Test Cases = | 168 |
| Module: | GWMINVRL | Number of Test Cases = | 40 |
| Module: | GWMKURS | Number of Test Cases = | 133 |
| Module: | GWMRAFWZ | Number of Test Cases = | 240 |
| Modules = | 167 | Number of Test Cases = | 58931 |

FIVS Test Case Quantity

| Test Case Quantity | | | |
|--------------------|------------------------------------|---|-------|
| FIVS | Total Number of Functions tested | = | 217 |
| FIVS | Total Number of Modules tested | = | 167 |
| FIVS | Total Number of Projects tested | = | 10 |
| FIVS | Total Number of System TestProcs | = | 259 |
| FIVS | Total Number of System TestCases | = | 13634 |
| FIVS | Total Number of Online TestCases | = | 5689 |
| FIVS | Total Number of Batch TestCases | = | 49 |
| FIVS | Total Number of Interfac TestCases | = | 7896 |
| FIVS | Total Number of Testcase Types | = | 7 |
| FIVS | Total Number of Test Deficiencies | = | 36309 |
| FIVS | Total Number of Major Deficiencies | = | 7645 |
| FIVS | Total Number of Media Deficiencies | = | 276 |
| FIVS | Total Number of Minor Deficiencies | = | 28388 |

FIVS Test Case Complexity & Quality

Test Case Complexity

| | | | | | | |
|--|------|----------|------------------------|---|-------|--|
| | FIVS | Testcase | Data Complexity Ratio | = | 0.765 | |
| | FIVS | Testcase | Test Density Ratio | = | 0.554 | |
| | FIVS | Testcase | Test Intensity Ratio | = | 0.810 | |
| | FIVS | Testcase | Test Volume Ratio | = | 0.231 | |
| | FIVS | Overall | Test Complexity Rating | = | 0.590 | |

Test Case Quality

| | | | | | | |
|--|------|----------|---------------------|---|-------|--|
| | FIVS | Testcase | Impact Ratio | = | 0.769 | |
| | FIVS | TestCase | Reusability Ratio | = | 0.432 | |
| | FIVS | TestCase | Conformity Ratio | = | 0.560 | |
| | FIVS | TestCase | Coverage Ratio | = | 0.984 | |
| | FIVS | Overall | Test Quality Rating | = | 0.686 | |

Calculating Test Costs

Primary factors for estimating Test costs

- Number of Test Cases required
- Testability of the Software
- Test Productivity = Test Cases/Tester Days

Estimating the Number of Test Cases

- **Blackbox-Test Cases** = {UseCases x Steps x Rules }
+ {GUI's x Objects x States }
+ {DB-Tables x Tuples x Instances }
- **Greybox-Test Cases** = {Interfaces x Parameters x Values }
- **Whitebox-Test Cases** = {Methods x Method Invocations }
+ {Objects x Object states }
| Control paths

Calculating Test Effort with COCOMO-II

$$\text{Test Effort} = \text{ST} \left\{ \frac{\text{Number Test Cases}}{\text{Test Productivity}} \right\}^{** \text{SE}} \times \text{Testability Factor}$$

Where ST = System Type (0,5:4)

and SE = Scaling Exponent (0,91:1,23)

$$\text{Testability Factor} = 0,5 / \text{Testability Ratio}$$

If the standard test productivity = 20 test cases per day and there are 1000 test cases to be tested and the testability ratio is 0.4 with a scaling exponent of 1,10 for a distributed system the testing effort will be:

$$(((1000/20 = 50) ** 1.10 = 74) \times 1.25 = 92.5) \times 2 = 185 \text{ Days}$$

Metrics for Measuring Test Coverage

Requirements Coverage = $\frac{\text{Tested Requirements}}{\text{Specified Requirements}}$

Architectural Coverage = $\frac{\text{Tested Architectural Features}}{\text{Architectural Features}}$

Code Coverage = $\frac{\text{Tested Statements, Branches, Paths}}{\text{Statements, Branches, Paths, States}}$

Test Case Coverage = $\frac{\text{Executed Test Cases}}{\text{Specified Test Cases}}$

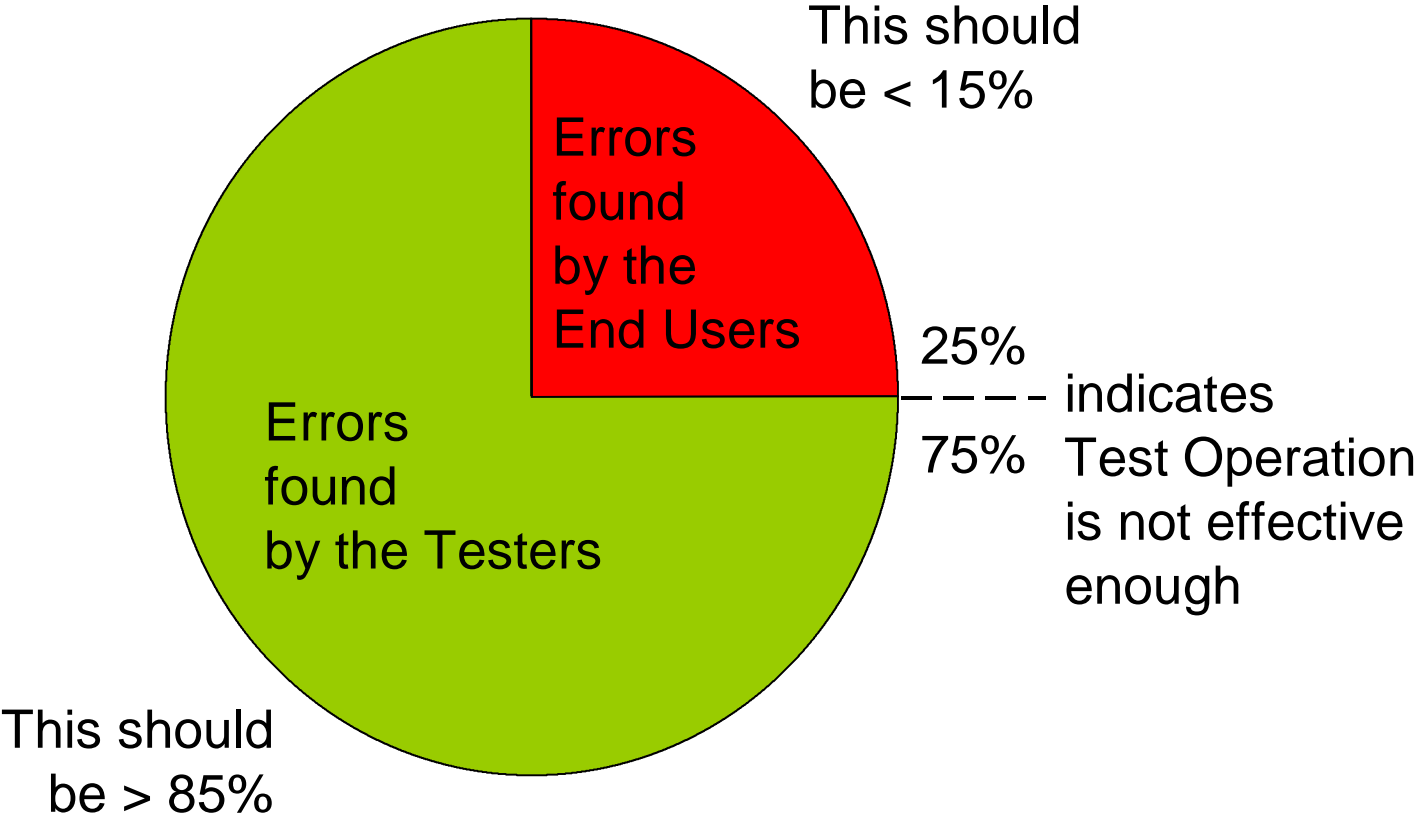
Metrics for evaluating Test Effectiveness

$$\text{Test Effectiveness} = \frac{\text{Weighted Errors reported by Testers}}{\text{Total weighted Errors reported}}$$

$$\text{Total weighted Errors} = \text{Tester reported} + \text{User reported Errors}$$

$$\text{Test Confidence} = 1 - \left\{ \frac{\text{weighted Errors}}{\text{executed Test Cases}} \right\} \times \text{Test Coverage Rate}$$

Ratio of Tester to User Error Reports



Test Metrics from the GEOS Project

| GUI Panels | Reports | Parameters | Test Data | TestCases (soll) | TestCases |
|------------|---------|------------|-----------|------------------|-----------|
| 225 | 94 | 674882 | 788384 | 39232 | 36735 |
| 363 | 400 | 307879 | 761315 | 38942 | 37521 |
| 67 | 28 | 37118 | 16862 | 2845 | 1411 |
| 35 | 46 | 3719 | 598 | 1703 | 1343 |
| 104 | 37 | 148796 | 78300 | 2177 | 2145 |
| 111 | 10 | 129220 | 95579 | 925 | 793 |
| 905 | 615 | 1301614 | 1741038 | 85824 | 79948 |

Defect Analysis in the GEOS Project

| Defects | Test Quality | Defect per Tc | DefectDensity | DefectDensity |
|---------|--------------|---------------|---------------|---------------|
| 897 | 0.829 | 0.119 | 0.013 | 0.0022 |
| 196 | 0.763 | 0.016 | 0.004 | 0.0001 |
| 140 | 0.851 | 0.501 | 0.002 | 0.0011 |
| 256 | 0.809 | 0.808 | 0.004 | 0.0022 |
| 10 | 0.901 | 0.088 | 0.001 | 0 |
| 36 | 0.684 | 0.098 | 0.001 | 0.0001 |
| 1535 | 0.722 | 0.088 | 0.014 | 0.0006 |
| | 0.822 | | | |
| | 0.178 | | | |

Comparison of SubSystems

Test Metric Conclusion

Five categories of Test Metrics have been presented here:

- Metrics for measuring Testability
- Metrics for assessing the quantity, quality & complexity of the Test Cases
- Metrics for calculating Test Costs
- Metrics for measuring Test Coverage
- Metrics for assessing the benefits of the Test Operation

More Research on Test Metrics required

The metrics presented here are intended to make testing more transparent. Testing has evolved into a major resource consumer and cost driver. Many managers are beginning to ask what they are getting for the money they are investing in testing. What are the benefits of testing? This study has offered two metrics for helping to answer that question. There are certainly others to be discovered. That is why this study can only be considered as a first step in the process of transforming software testing from an art into a science. With more research coupled with empirical studies it may someday even be possible to understand what we are doing according to the criteria of Lord Kelvin.